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MATHEMATICS
Paper 1
2024



UGANDA NATIONAL EXAMINATIONS BOARD
Uganda Certificate of Education

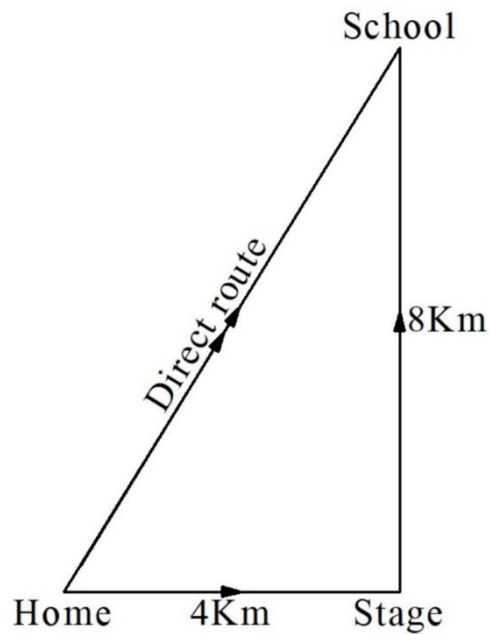
MATHEMATICS

Paper 1

New Lower Secondary Curriculum

SCORING GUIDE

1(a) Distance from home to school using the direct route.



$$(\text{Direct distance})^2 = 4^2 + 8^2$$

$$\begin{aligned} \text{Direct distance} &= \sqrt{4^2 + 8^2} \\ &= \sqrt{16 + 64} \\ &= \sqrt{80} \\ &= 8.94\text{km} \end{aligned}$$

$$\begin{aligned} \text{(b)(i) school fees} &= \frac{100-60}{100} \times 900,000/= \\ &= \frac{40}{100} \times 900,000/= \\ &= 360,000/= \end{aligned}$$

$$\begin{aligned} \text{Uniform} &= 350,000 - 87,500 \\ &= 262,500/= \end{aligned}$$

$$\begin{aligned} \text{Total amount to be paid} &= 360,000 + 262,500 \\ &= 622,500/= \end{aligned}$$

(b)(ii) Conclusion: yes, the guardian will afford the school since the total amount to be paid is less than the 700,000/= s/he has budgeted for school expenses.

(c)(i) Payment plan 1

$$\begin{aligned}\text{First instalment} &= \frac{2}{3} \times 900,000/= \\ &= 600,000/= \end{aligned}$$

$$\begin{aligned}\text{Second instalment} &= 900,000 - 600,000 \\ &= 300,000/= \end{aligned}$$

Payment plan 2

$$\begin{aligned}\text{Each instalment} &= \frac{1}{3} \times 900,000/= \\ &= 300,000/= \end{aligned}$$

(c)(ii) Recommended payment plan:

Reason:

2. Let x be the number of cows to be sold and y the number of goats to be sold.

$$x \geq 0, y \geq 0$$

$$x \leq 10$$

$$y \geq 8$$

$$x + y \leq 20$$

$$y < 2x$$

$$\text{Sales} = 1,500,000x + 200,000y$$

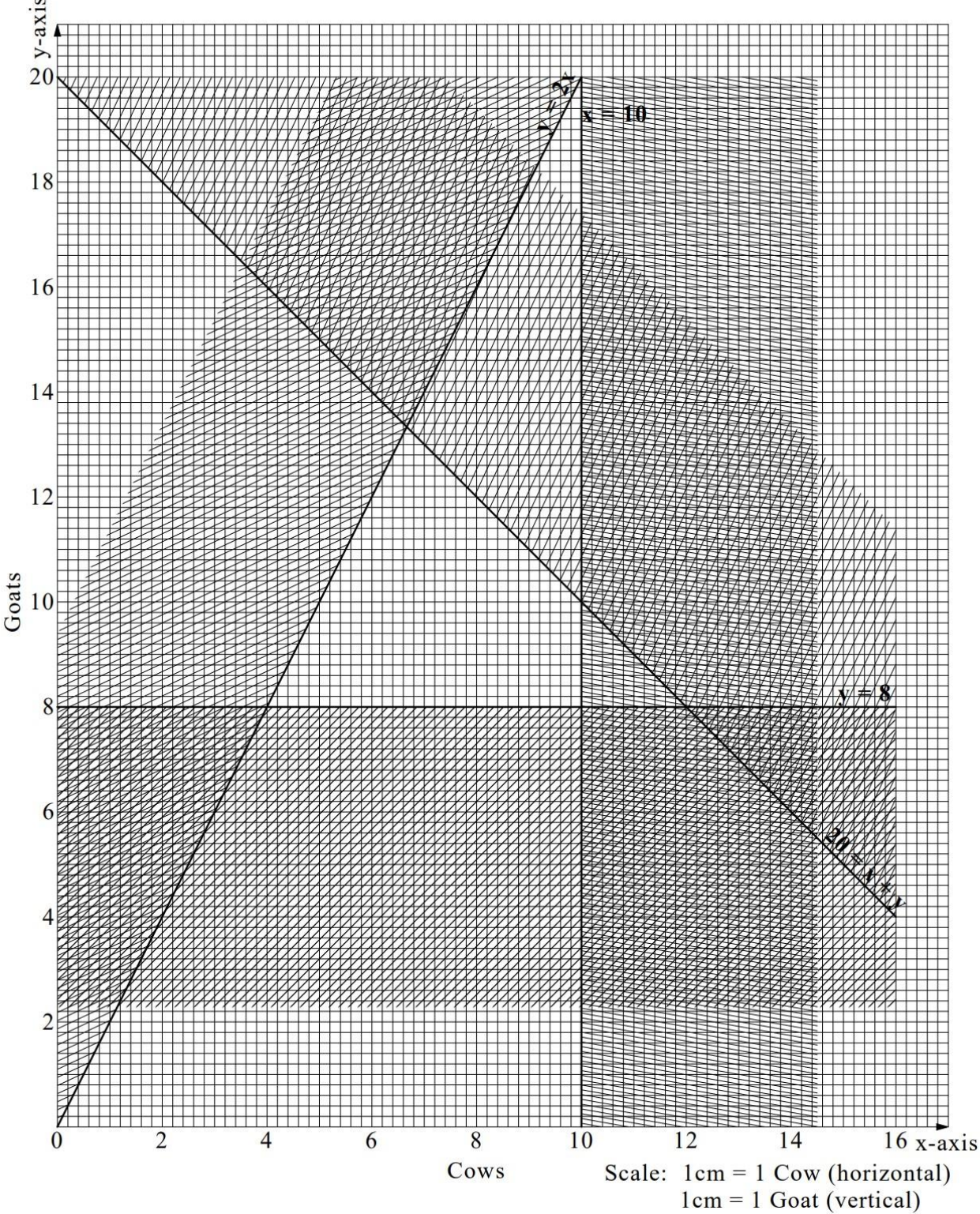
$$\text{For } y = 2x$$

x	0	1
y	0	2

$$\text{For } x + y = 20$$

x	0	20
y	20	0

A graph showing the feasible region



Maximisation of sales

Optimal points (x,y)	Sales =1,500,000x + 200,000y
(10,10)	17,000,000
(9,11)	15,700,000
(8,12)	14,000,000
(7,13)	13,100,000

(any other point(s) within the feasible region)

Conclusion: Chooses a combination that maximises sales (a combination that gives the highest amount of money).

That is,they should sell ten cows and ten goats to maximise sales and they will make 17,000,000/=.

OR

Accept any other correct method.

Qtn3.

Time(Min)	Tallies	Freq (f)	Cumm freq	Class boundary	Mid-point (x)	fx
15-19	///	3	3	14.5-19.5	17	51
20-24	////	4	7	19.5-24.5	22	88
25-29	### ///	10	17	24.5-29.5	27	270
30-34	### ///	11	28	29.5-34.5	32	352
35-39	### ////	9	37	34.5-39.5	37	333
40-44	### /	6	43	39.5-44.5	42	252
45-49	### //	7	50	44.5-49.5	47	329
50-54	###	5	55	49.5-54.5	52	260
55-59	###	5	60	54.5-59.5	57	285
		$\Sigma f=60$				$\Sigma fx=2220$

(a) Mean time = $\frac{\Sigma fx}{\Sigma f} = \frac{2220}{60} = 37$ minutes

The assemble start time should be 37 minutes from 7:30AM since the average time of arrival of the students after 7:30 AM is 37 minutes. That is, the assembly should start at 8:07 AM.

Note: Accept calculation of any measure of central tendency followed by a relevant/appropriate explanation.

(b) EITHER

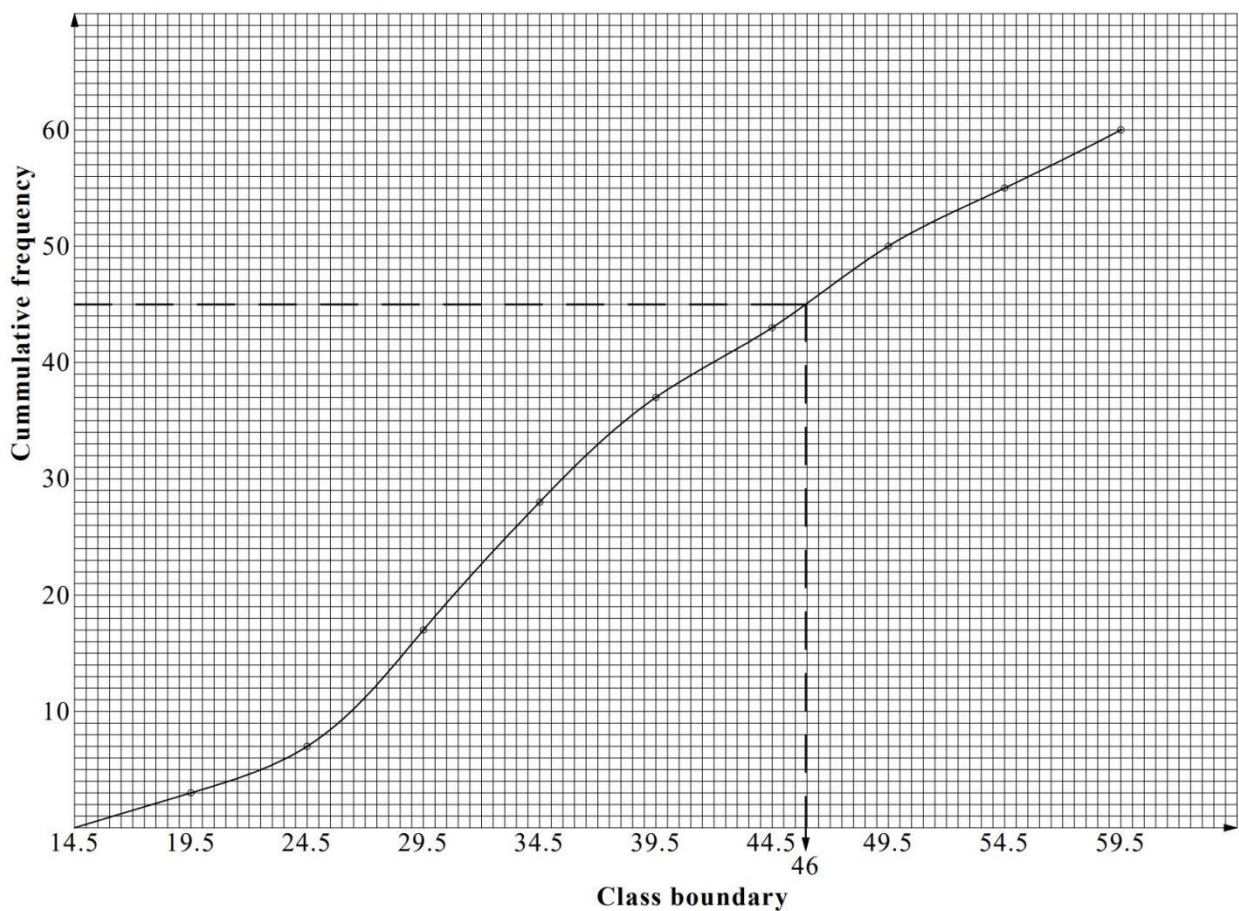
75% = 75th percentile, given by $(\frac{75}{100} \times N)^{\text{th}}$ position of cumulative frequency.

= $(\frac{75}{100} \times 60)^{\text{th}}$ position of cumulative frequency

= 45th position of cumulative frequency

From the Ogive, 75th percentile = 46 minutes. (see Ogive)

The assemble start time should be 46 minutes from 7:30AM since the arrival time of 75% of the students after 7:30AM is 46 minutes. That is, the assembly should start at 8:16AM.



OR

Note: Accept calculation of the 75th percentile using a formula.

Question 4

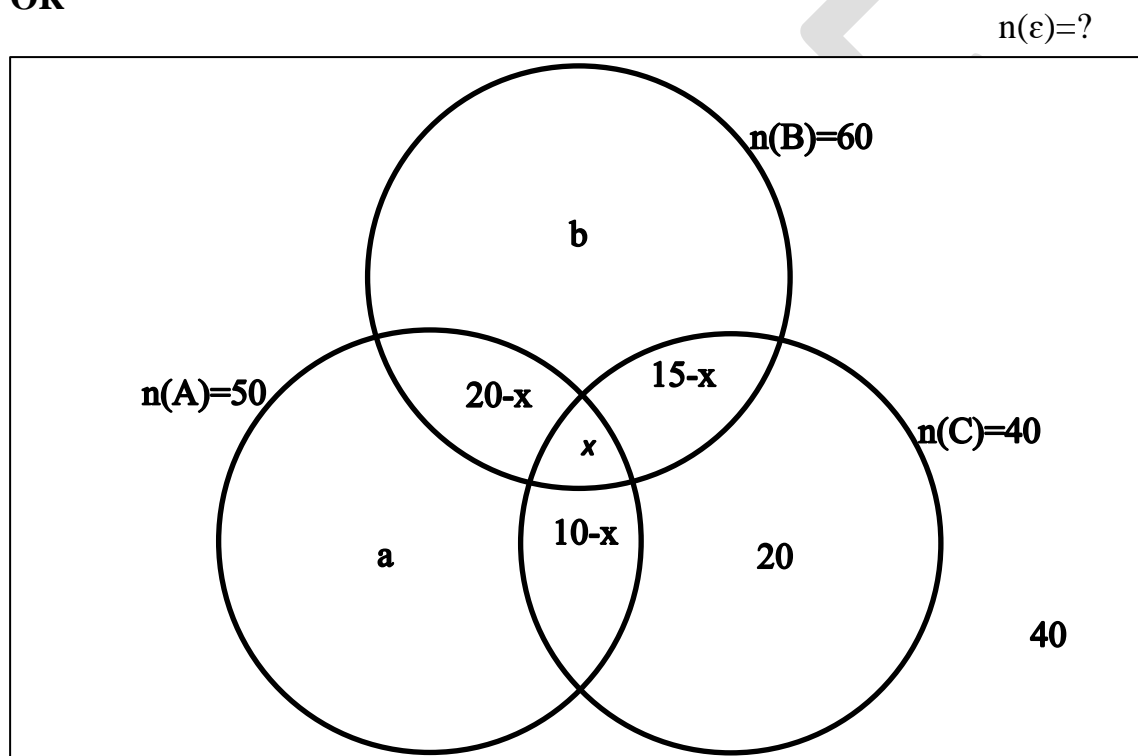
SOLUTION

EITHER

$n(\epsilon)=?$, $n(A)=50$, $n(B)=60$, $n(C)=40$, $n(A \cap B)=20$, $n(A \cap C)=10$, $n(B \cap C)=15$, $n(C)_{\text{only}}=20$,

$n(A \cap B \cap C)=x$, $n(A \cap B)_{\text{only}}=20-x$, $n(A \cap C)_{\text{only}}=10-x$, $n(B \cap C)_{\text{only}}=15-x$, $n(A)_{\text{only}}=?$, $n(B)_{\text{only}}=?$,
 $n(A \cup B \cup C)' = 40$.

OR



Using the people who visited district C and tested positive gives;

$$x + 15 - x + 10 - x + 20 = 40$$

$$45 - x = 40$$

$$x = 5$$

Therefore, 5 people who had visited all the three districts tested positive for malaria.

The number of people who visited district A only and tested positive is given by;

$$50 - (x + 20 - x + 10 - x) = 50 - 30 + x = 20 + 5 = 25$$

The number of people who visited district B only and tested positive is given by;

$$60 - (x + 20 - x + 15 - x) = 60 - 35 + x = 25 + 5 = 30$$

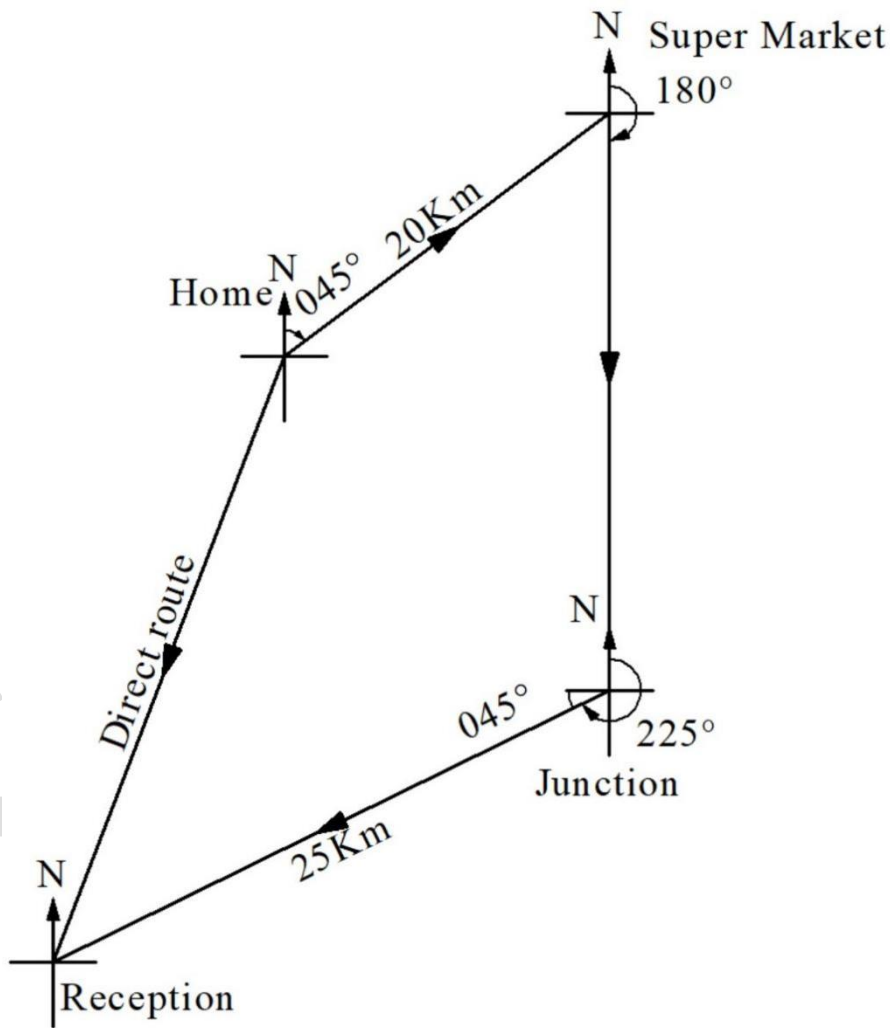
The number of people who visited at least one district and tested positive is given by;
 $60 + 25 + (10 - x) + 20 = 115 - x = 115 - 5 = 110$

The sample that was purposively selected $n(\epsilon) = 110 + 40 = 150$

Therefore the chance of testing positive for malaria having visited at least one district is given by;
 $P(\text{positive having visited at least one district}) = \frac{110}{150} = 0.733 = 73.3\%$

The ministry should come up with interventions since the chance of testing positive having visited at least one district is high (73.3%).

5. Sketch drawing



Distance (D) from super market to junction?

Speed = 50km/h

Time = 45minutes

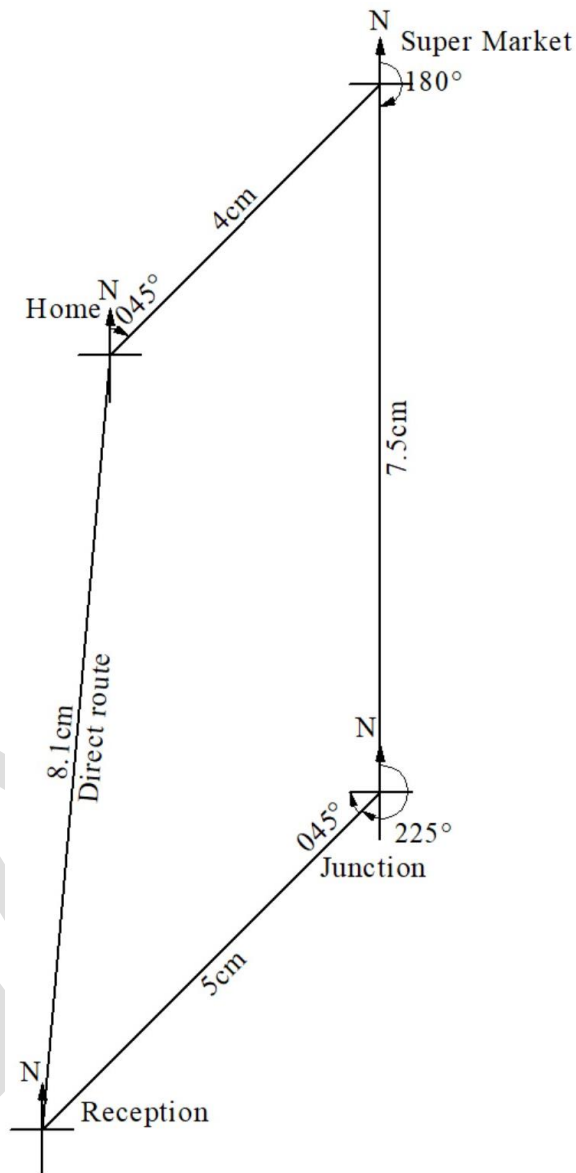
$$= \frac{45}{60} \text{ hours or Time} = \frac{3}{4} \text{ hours or Time} = 0.75 \text{ hours}$$

$$D = \text{Speed} \times \text{Time}$$

$$D = 50 \times 0.75$$

$$D = 37.5 \text{ km}$$

Accurate drawing



(a)(i) State the bearing of the Home from the Reception.

(a)(ii) Direct route distance = 8.1 cm

$$= (8.1 \times 5) \text{ km}$$

$$= 40.5 \text{ km}$$

(ii) Distance = 40.5 km

Speed = 50 km/h

$$\text{Time} = \frac{\text{Distance}}{\text{Speed}}$$

$$\text{Time} = \frac{40.5}{50}$$

Time = 0.81 hours

Time = (0.81 × 60) minutes

Time = 48.6 minutes

Time ≈ 49 minutes

We will leave home 49 minutes to 2:00 PM to reach the party venue on time.

OR

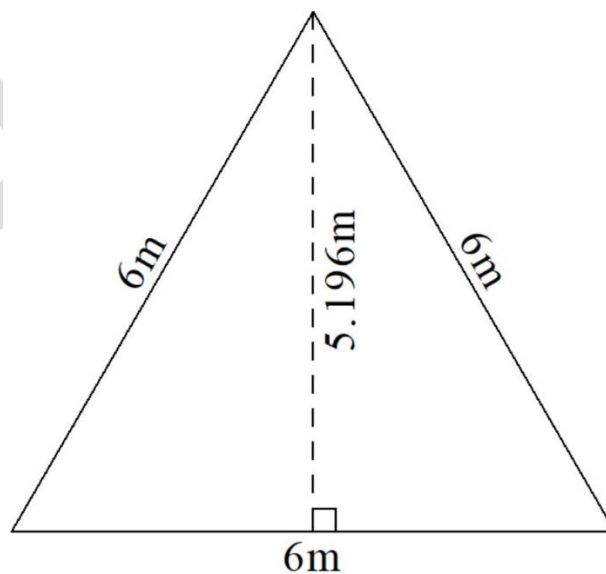
We will leave home at 1:11 PM = (2:00 PM – 49 Minute) to reach the party venue on time.

QUESTION 6

Area of the triangular sides

$$\text{Height (h) of the triangular side} = \sqrt{6^2 - 3^2}$$

$$= 5.196\text{m or } (\sqrt{27})\text{m or } (3\sqrt{3})\text{m}$$

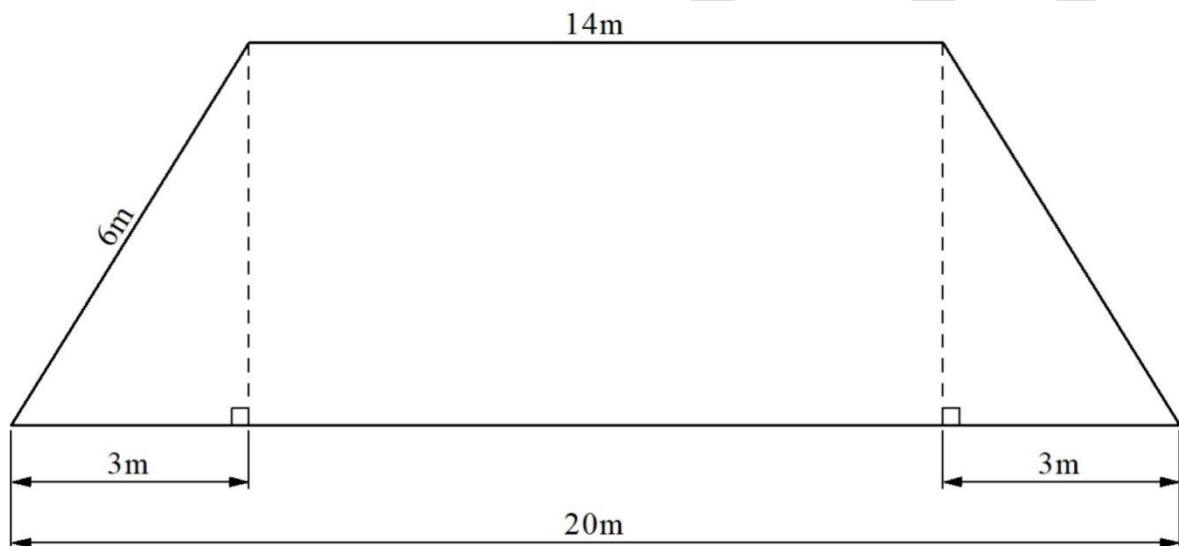


$$\begin{aligned}
 \text{Area of one triangular side} &= \frac{1}{2} \times \text{base} \times \text{height} \\
 &= \frac{1}{2} \times 6 \times 5.196 \\
 &= 15.588\text{m}^2
 \end{aligned}$$

$$\begin{aligned}
 \text{Area of the two triangular sides} &= 2 \times 15.588 \\
 &= 31.176\text{m}^2
 \end{aligned}$$

Note: Accept any method of finding the area of the triangular side.

Area of the trapezium sides



$$\begin{aligned}
 \text{Height}(h)\text{of the trapezium} &= \sqrt{(6^2 - 3^2)} \\
 &= 5.196\text{m or } (\sqrt{27})\text{m or } (3\sqrt{3})\text{m}
 \end{aligned}$$

$$\begin{aligned}
 \text{Area of one trapezium side} &= \frac{1}{2} \times h (a + b) \\
 &= \frac{1}{2} \times 5.196 (14 + 20) \\
 &= 88.332\text{m}^2
 \end{aligned}$$

$$\begin{aligned}
 \text{Area of the two trapezium sides} &= 2 \times 88.332 \\
 &= 176.664\text{m}^2
 \end{aligned}$$

$$\begin{aligned}
 \text{Total area of the roof} &= 31.176 + 176.664 \\
 &= 207.84\text{m}^2
 \end{aligned}$$

OR

Advise: My neighbour should buy Type B iron sheets.

Reason: Since they are expensive, they are likely to be of a better quality than Type A.

			SCORE
1	TOTAL AREA OF THE ROOF		
(a)	Area of the triangular side		Subtotal- 04
(i)	Height		01
(ii)	Substitution for Area		01
(iii)	Area	value	01
		unit	01
(b)	Area of the trapezium side		Subtotal-04
	Height		02
	Area	Use of formula	01
		Value	01
(c)	Total area of the roof	operation	01
		Correct value	01
2	Usable area of the iron sheet	Correct Value	01
3	Conversion of units	Correct value	01
4	Number of iron sheets	operation	01
		Correct value	01
		Actual number	01
5	Cost of the iron sheets		Subtotal-03
	Correct total cost without discount		01
	Discounted cost	operation	01
		Correct value (for either)	01
			Subtotal-02
6	Advice/Justification	Type of iron sheet	01
		Reason	01
TOTAL SCORE			20